

IDENTIFY COMPUTE INTERPRET

GERALD
KELLER

Statistics

for Management and Economics

10e

A GUIDE TO STATISTICAL TECHNIQUES

Problem Objectives

	Describe a Population	Compare Two Populations	Compare Two or More Populations	Analyze Relationship between Two Variables	Analyze Relationship among Two or More Variables
Interval	<p>Histogram Section 3-1</p> <p>Ogive Section 3-1</p> <p>Stem-and-leaf Section 3-1</p> <p>Line chart Section 3-2</p> <p>Mean, median, and mode Section 4-1</p> <p>Range, variance, and standard deviation Section 4-2</p> <p>Percentiles and quartiles Section 4-3</p> <p>Box plot Section 4-3</p> <p>t-test and estimator of a mean Section 12-1</p> <p>Chi-squared test and estimator of a variance Section 12-2</p>	<p>Equal-variances t-test and estimator of the difference between two means: independent samples Section 13-1</p> <p>Unequal-variances t-test and estimator of the difference between two means: independent samples Section 13-1</p> <p>t-test and estimator of mean difference Section 13-3</p> <p>F-test and estimator of ratio of two variances Section 13-4</p> <p>Wilcoxon rank sum test Section 19-1</p> <p>Wilcoxon signed rank sum test Section 19-2</p>	<p>One-way analysis of variance Section 14-1</p> <p>LSD multiple comparison method Section 14-2</p> <p>Tukey's multiple comparison method Section 14-2</p> <p>Two-way analysis of variance Section 14-4</p> <p>Two-factor analysis of variance Section 14-5</p> <p>Kruskal-Wallis test Section 19-3</p> <p>Friedman test Section 19-3</p>	<p>Scatter diagram Section 3-3</p> <p>Covariance Section 4-4</p> <p>Coefficient of correlation Section 4-4</p> <p>Coefficient of determination Section 4-4</p> <p>Least squares line Section 4-4</p> <p>Simple linear regression and correlation Chapter 16</p> <p>Spearman rank correlation Section 19-4</p>	<p>Multiple regression Chapters 17 & 18</p>
Nominal	<p>Frequency distribution Section 2-2</p> <p>Bar chart Section 2-2</p> <p>Pie chart Section 2-2</p> <p>z-test and estimator of a proportion Section 12-3</p> <p>Chi-squared goodness-of-fit test Section 15-1</p>	<p>z-test and estimator of the difference between two proportions Section 13-5</p> <p>Chi-squared test of a contingency table Section 15-2</p>	<p>Chi-squared test of a contingency table Section 15-2</p>	<p>Chi-squared test of a contingency table Section 15-2</p>	<p>Not covered</p>
Ordinal	<p>Median Section 4-1</p> <p>Percentiles and quartiles Section 4-3</p> <p>Box plot Section 4-3</p>	<p>Wilcoxon rank sum test Section 19-1</p> <p>Sign test Section 19-2</p>	<p>Kruskal-Wallis test Section 19-3</p> <p>Friedman test Section 19-3</p>	<p>Spearman rank correlation Section 19-4</p>	<p>Not covered</p>

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for Management and Economics

10e

GERALD KELLER

Professor Emeritus, Wilfrid Laurier University



Australia • Brazil • Japan • Korea • Mexico • Singapore • Spain • United Kingdom • United States

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PREFACE

Businesses are increasingly using statistical techniques to convert data into information. For students preparing for the business world, it is not enough merely to focus on mastering a diverse set of statistical techniques and calculations. A course and its attendant textbook must provide a complete picture of statistical concepts and their applications to the real world. *Statistics for Management and Economics* is designed to demonstrate that statistics methods are vital tools for today's managers and economists.

Fulfilling this objective requires the several features that I have built into this book. First, I have included data-driven examples, exercises, and cases that demonstrate statistical applications that are and can be used by marketing managers, financial analysts, accountants, economists, operations managers, and others. Many are accompanied by large and either genuine or realistic data sets. Second, I reinforce the applied nature of the discipline by teaching students how to choose the correct statistical technique. Third, I teach students the concepts that are essential to interpreting the statistical results.

Why I Wrote This Book

Business is complex and requires effective management to succeed. Managing complexity requires many skills. There are more competitors, more places to sell products, and more places to locate workers. As a consequence, effective decision making is more crucial than ever before. On the other hand, managers have more access to larger and more detailed data that are potential sources of information. However, to achieve this potential requires that managers know how to convert data into information. This knowledge extends well beyond the arithmetic of calculating statistics. Unfortunately, this is what most textbooks offer—a series of unconnected techniques illustrated mostly with manual calculations. This continues a pattern that goes back many years. What is required is a complete approach to applying statistical techniques.

When I started teaching statistics in 1971, books demonstrated how to calculate statistics and, in some cases, how various formulas were derived. One reason for doing so was the belief that by doing calculations by hand, students would be able to understand the techniques and concepts. When the first edition of this book was published in 1988, an important goal was to teach students to identify the correct technique. Through the next nine editions, I refined my approach to emphasize interpretation and decision making equally. I now divide the solution of statistical problems into three stages and include them in every appropriate example: (1) *identify* the technique, (2) *compute* the statistics, and (3) *interpret* the results. The compute stage can be completed in any or all of three ways: manually (with the aid of a calculator), using Excel, and using Minitab. For those courses that wish to use the computer extensively, manual calculations can be played down or omitted completely. Conversely, those that wish to emphasize manual calculations may easily do so, and the computer solutions can be selectively introduced or skipped entirely. This approach is designed to provide maximum flexibility, and it leaves to the instructor the decision of if and when to introduce the computer.

I believe that my approach offers several advantages:

- An emphasis on identification and interpretation provides students with practical skills they can apply to real problems they will face regardless of whether a course uses manual or computer calculations.
- Students learn that statistics is a method of converting data into information. With 967 data files and corresponding problems that ask students to interpret statistical results, students are given ample opportunities to practice data analysis and decision making.
- The optional use of the computer allows for larger and more realistic exercises and examples.

Placing calculations in the context of a larger problem allows instructors to focus on more important aspects of the decision problem. For example, more attention needs to be devoted to interpreting statistical results. Proper interpretation of statistical results requires an understanding of the probability and statistical concepts that underlie the techniques and an understanding of the context of the problems. An essential aspect of my approach is teaching students the concepts. I do so by providing instructions about how to create Excel worksheets that allow students to perform “what-if” analyses. Students can easily see the effect of changing the components of a statistical technique, such as the effect of increasing the sample size.

Efforts to teach statistics as a valuable and necessary tool in business and economics are made more difficult by the positioning of the statistics course in most curricula. The required statistics course in most undergraduate programs appears in the first or second year. In many graduate programs, the statistics course is offered in the first semester of a three-semester program and the first year of a two-year program. Accounting, economics, finance, human resource management, marketing, and operations management are usually taught after the statistics course. Consequently, most students will not be able to understand the general context of the statistical application. This deficiency is addressed in this book by “Applications in ...” sections, subsections, and boxes. Illustrations of statistical applications in business that students are unfamiliar with are preceded by an explanation of the background material.

- For example, to illustrate graphical techniques, we use an example that compares the histograms of the returns on two different investments. To explain what financial analysts look for in the histograms requires an understanding that risk is measured by the amount of variation in the returns. The example is preceded by an “Applications in Finance” box that discusses how return on investment is computed and used.
- Later when I present the normal distribution, I feature another “Applications in Finance” box to show why the standard deviation of the returns measures the risk of that investment.
- Thirty-six application boxes are scattered throughout the book.

Some applications are so large that I devote an entire section or subsection to the topic. For example, in the chapter that introduces the confidence interval estimator of a proportion, I also present market segmentation. In that section, I show how the confidence interval estimate of a population proportion can yield estimates of the sizes of market segments. In other chapters, I illustrate various statistical techniques by showing how marketing managers can apply these techniques to determine the differences that exist between market segments. There are six such sections and one subsection in this book.

The “Applications in ...” segments provide great motivation to the student who asks, “How will I ever use this technique?”

New in This Edition

Eight large real data sets are the sources of 369 new exercises. Students will have the opportunity to convert real data into information. Instructors can use the data sets for hundreds of additional examples and exercises.

Many of the examples, exercises, and cases using real data in the ninth edition have been updated. These include the data on wins, payrolls, and attendance in baseball, basketball, football, and hockey; returns on stocks listed on the New York Stock Exchange, NASDAQ, and Toronto Stock Exchange; and global warming.

I’ve created many new examples and exercises. Here are the numbers for the tenth edition: 145 solved examples, 2148 exercises, 27 cases, 967 data sets, 35 appendixes containing 37 solved examples, 98 exercises, and 25 data sets, for a grand total of 182 worked examples, 2246 exercises, 27 cases, and 992 data sets.

Data Driven: The Big Picture

Solving statistical problems begins with a problem and data. The ability to select the right method by problem objective and data type is a **valuable tool for business**. Because business decisions are driven by data, students will leave this course equipped with the tools they need to make effective, informed decisions in all areas of the business world.



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Identify the Correct Technique

Examples introduce the first crucial step in this three-step (*identify–compute–interpret*) approach. Every example’s solution begins by examining the data type and problem objective and then identifying the right technique to solve the problem.

EXAMPLE 13.1*

DATA
Xm13-01

Direct and Broker-Purchased Mutual Funds

Millions of investors buy mutual funds (see page 178 for a description of mutual funds), choosing from thousands of possibilities. Some funds can be purchased directly from banks or other financial institutions whereas others must be purchased through brokers, who charge a fee for this service. This raises the question, Can investors do better by buying mutual funds directly than by purchasing mutual funds through brokers? To help answer this question, a group of researchers randomly sampled the annual returns from mutual funds that can be acquired directly and mutual funds that are bought through brokers and recorded the net annual returns, which are the returns on investment after deducting all relevant fees. These are listed next.

Direct					Broker				
9.33	4.68	4.23	14.69	10.29	3.24	3.71	16.4	4.36	9.43
6.94	3.09	10.28	-2.97	4.39	-6.76	13.15	6.39	-11.07	8.31
16.17	7.26	7.1	10.37	-2.06	12.8	11.05	-1.9	9.24	-3.99
16.97	2.05	-3.09	-0.63	7.66	11.1	-3.12	9.49	-2.67	-4.44
5.94	13.07	5.6	-0.15	10.83	2.73	8.94	6.7	8.97	8.63
12.61	0.59	5.27	0.27	14.48	-0.13	2.74	0.19	1.87	7.06
3.33	13.57	8.09	4.59	4.8	18.22	4.07	12.39	-1.53	1.57
16.13	0.35	15.05	6.38	13.12	-0.8	5.6	6.54	5.23	-8.44
11.2	2.69	13.21	-0.24	-6.54	-5.75	-0.85	10.92	6.87	-5.72
1.14	18.45	1.72	10.32	-1.06	2.59	-0.28	-2.15	-1.69	6.95

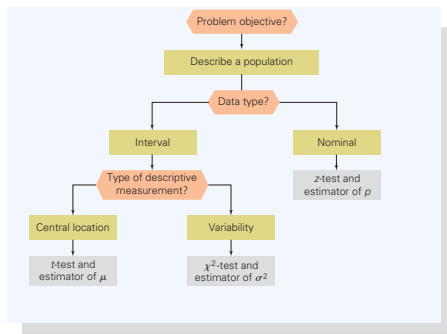
Can we conclude at the 5% significance level that directly purchased mutual funds outperform mutual funds bought through brokers?

SOLUTION:

IDENTIFY

To answer the question, we need to compare the population of returns from direct and the returns from broker-bought mutual funds. The data are obviously interval (we’ve recorded real numbers). This problem objective–data type combination tells us that the parameter to be tested is the difference between two means, $\mu_1 - \mu_2$. The hypothesis

*Source: D. Bergstresser, J. Chalmers, and P. Tufano, “Assessing the Costs and Benefits of Brokers in the Mutual Fund Industry.”



Appendices 13, 14, 15, 16, 17, and 19 reinforce this problem-solving approach and allow students to hone their skills.

Flowcharts, found within the appendices, help students develop the logical process for choosing the correct technique, reinforce the learning process, and provide easy review material for students.

APPENDIX 14 / REVIEW OF CHAPTERS 12 TO 14

The number of techniques introduced in Chapters 12 to 14 is up to 20. As we did in Appendix 13, we provide a table of the techniques with formulas and required conditions, a flowchart to help you identify the correct technique, and 25 exercises to give you practice in how to choose the appropriate method. The table and the flowchart have been amended to include the three analysis of variance techniques introduced in this chapter and the three multiple comparison methods.

TABLE A14.1 Summary of Statistical Techniques in Chapters 12 to 14

t-test of μ
Estimator of μ (including estimator of $N\mu$)
χ^2 test of σ^2
Estimator of σ^2
z-test of ρ
Estimator of ρ (including estimator of $N\rho$)
Equal-variances t-test of $\mu_1 - \mu_2$
Equal-variances estimator of $\mu_1 - \mu_2$
Unequal-variances t-test of $\mu_1 - \mu_2$
Unequal-variances estimator of $\mu_1 - \mu_2$
t-test of μ_D
Estimator of μ_D
F-test of σ_1^2/σ_2^2
Estimator of σ_1^2/σ_2^2
z-test of $\rho_1 - \rho_2$ (Case 1)
z-test of $\rho_1 - \rho_2$ (Case 2)
Estimator of $\rho_1 - \rho_2$
One-way analysis of variance (including multiple comparisons)
Two-way (randomized blocks) analysis of variance
Two-factor analysis of variance

Factors That Identify the Independent Samples Two-Factor Analysis of Variance

1. **Problem objective:** Compare two or more populations (populations are defined as the combinations of the levels of two factors)
2. **Data type:** Interval
3. **Experimental design:** Independent samples

Factors That Identify ... boxes are found in each chapter after a technique or concept has been introduced. These boxes allow students to see a technique's essential requirements and give them a way to easily review their understanding. These essential requirements are revisited in the review chapters, where they are coupled with other concepts illustrated in flowcharts.

A Guide to Statistical Techniques, found on the inside front cover of the text, pulls everything together into one useful table that helps students identify which technique to perform based on the problem objective and data type.

A GUIDE TO STATISTICAL TECHNIQUES				
<i>Problem Objectives</i>				
		Describe a Population	Compare Two Populations	Compare Two or More Populations
DATA TYPES	Interval	Histogram Section 3-1 Ogive Section 3-1 Stem-and-leaf Section 3-1 Line chart Section 3-2 Mean, median, and mode Section 4-1 Range, variance, and standard deviation Section 4-2 Percentiles and quartiles Section 4-3 Box plot Section 4-3 t -test and estimator of a mean Section 12-1 Chi-squared test and estimator of a variance Section 12-2	Equal-variances t -test and estimator of the difference between two means: independent samples Section 13-1 Unequal-variances t -test and estimator of the difference between two means: independent samples Section 13-1 t -test and estimator of mean difference Section 13-3 F -test and estimator of ratio of two variances Section 13-4 Wilcoxon rank sum test Section 19-1 Wilcoxon signed rank sum test Section 19-2	One-way analysis of variance Section 14-1 LSD multiple comparison method Section 14-2 Tukey's multiple comparison method Section 14-2 Two-way analysis of variance Section 14-4 Two-factor analysis of variance Section 14-5 Kruskal-Wallis test Section 19-3 Friedman test Section 19-3
	Nominal	Frequency distribution Section 2-2 Bar chart Section 2-2 Pie chart Section 2-2 z -test and estimator of a proportion Section 12-3 Chi-squared goodness-of-fit test Section 15-1	z -test and estimator of the difference between two proportions Section 13-5 Chi-squared test of a contingency table Section 15-2	Chi-squared test of a contingency table Section 15-2
	Ordinal	Median Section 4-1 Percentiles and quartiles Section 4-3 Box plot Section 4-3	Wilcoxon rank sum test Section 19-1 Sign test Section 19-2	Kruskal-Wallis test Section 19-3 Friedman test Section 19-3

More Data Sets

DATA
Xm13-02

A total of 967 data sets available to be downloaded provide ample practice. These data sets often contain real data, are typically large, and are formatted for Excel, Minitab, SPSS, SAS, JMP IN, and ASCII.

Prevalent use of data in examples, exercises, and cases is highlighted by the accompanying data icon, which alerts students to go to Keller’s website.

bought their newspapers from a street vendor and people who had the newspaper delivered to their homes. Each was asked how many minutes they spent reading their newspapers. Can we infer that the amount of time reading differs between the two groups?

13.190 Xm13-190 In recent years, a number of state governments have passed mandatory seat-belt laws. Although the use of seat belts is known to save lives and reduce serious injuries, compliance with seat-belt laws is not universal. In an effort to increase the use of seat belts, a government agency sponsored a 2-year study. Among its objectives was to determine whether there was enough evidence to infer that seat-belt usage increased between last year and this year. To test this belief, random samples of drivers last year and this year were asked whether they always use their seat belts (2 = Wear seat belt, 1 = Do not wear seat belt). Can we infer that seat belt usage has increased over the last year?

13.191 Xm13-191 An important component of the cost of living is the amount of money spent on housing. Housing costs include rent (for tenants), mortgage payments and property tax (for home owners), heating, electricity, and water. An economist undertook a 5-year study to determine how housing costs have changed. Five years ago, he took a random sample of 200 households and recorded the percentage of total income spent on housing. This year, he took another sample of 200 households.

- Conduct a test (with $\alpha = .10$) to determine whether the economist can infer that housing cost as a percentage of total income has increased over the last 5 years.
- Use whatever statistical method you deem appropriate to check the required condition(s) of the test used in part (a).

13.192 Xm13-192 In designing advertising campaigns to sell magazines, it is important to know how much time each of a number of demographic groups spend reading magazines. In a preliminary study, 40 people were randomly selected. Each was asked how much time per week he or she spends reading magazine. Additionally, each was categorized by gender and l

b. Is there sufficient evidence at the 10% significance level to conclude that high-income individuals devote more time to reading than low-income people?

13.193 Xm13-193 In a study to determine whether the highest salary offered affects salary offers for graduates, 25 pairs of students were selected. Each pair consisted of a female and a male who had matched according to their gender, courses taken, ages, and previous experience. The highest salary offered (in thousands of dollars) to each graduate was recorded.

- Is there enough evidence to infer that gender affects salary offers?
- Discuss why the experimenter matched the way it was.
- Is the required condition for the test satisfied?

13.194 Xm13-194 Have North Americans grown to distrust television and newspaper journalists? A study was conducted this year to compare what Americans currently think of the press versus what they said 3 years ago. The survey asked respondents whether they agreed that the press tends to favor one side when reporting on political and social issues. A random sample of people was asked to participate in this year’s survey. The results of a survey of another random sample taken 3 years ago are also available. The responses are 2 = Agree and 1 = Disagree. Can we conclude at the 10% significance level that Americans have become more distrustful of television and newspaper reporting this year than they

DATA
Xm13-09

EXAMPLE 13.9 Test Marketing of Package Designs, Part 1

The General Products Company produces and sells a variety of household products. Because of stiff competition, one of its products, a bath soap, is not selling well. Hoping to improve sales, General Products decided to introduce more attractive packaging. The company’s advertising agency developed two new designs. The first design features several bright colors to distinguish it from other brands. The second design is light green in color with just the company’s logo on it. As a test to determine which design is better, the marketing manager selected two supermarkets. In one supermarket, the soap was packaged in a box using the first design; in the second supermarket, the second design was used. The product scanner at each supermarket tracked every buyer of soap over a 1-week period. The supermarkets recorded the last four digits of the scanner code for each of the five brands of soap the supermarket sold. The code for the General Products brand of soap is 9077 (the other codes are 4255, 3745, 7118, and 8855). After the trial period, the scanner data were transferred to a computer file. Review the first

DATA
C14-01


CASE 14.1 Comparing Three Methods of Treating Childhood Ear Infections*

Acute otitis media, an infection of the middle ear, is a common childhood illness. There are various ways to treat the problem. To help determine the best way, researchers conducted an experiment. One hundred and eighty children between 10 months and 2 years with recurrent acute otitis media were divided into three equal groups. Group 1 was treated by surgically removing the adenoids (adenoidectomy), the second was treated with the drug Sulfafurazole, and the third with a placebo.

Each child was tracked for 2 years, during which time all symptoms and episodes of acute otitis media were recorded. The data were recorded in the following way:

<p>Column 1: ID number</p> <p>Column 2: Group number</p> <p>Column 3: Number of episodes of the illness</p> <p>Column 4: Number of visits to a physician because of any infection</p> <p>Column 5: Number of prescriptions</p> <p>Column 6: Number of days with symptoms of respiratory infection</p>	<ol style="list-style-type: none"> Are there differences between the three groups with respect to the number of episodes, number of physician visits, number of prescriptions, and number of days with symptoms of respiratory infection? Assume that you are working for the company that makes the drug Sulfafurazole. Write a report to the company’s executives discussing your results.
-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------	----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------

*This case is adapted from the *British Medical Journal*, February 2004.



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Flexible to Use

Although many texts today incorporate the use of the computer, *Statistics for Management and Economics* is designed for maximum flexibility and ease of use for both instructors and students. To this end, parallel illustration of both manual and computer printouts is provided throughout the text. This approach allows you to choose which, if any, computer program to use. Regardless of the method or software you choose, the output and instructions that you need are provided!

Compute the Statistics

Once the correct technique has been identified, examples take students to the next level within the solution by asking them to compute the statistics.

COMPUTE

MANUALLY:

From the data, we calculated the following statistics:

$s_1^2 = 37.49$ and $s_2^2 = 43.34$

Test statistic: $F = s_1^2/s_2^2 = 37.49/43.34 = 0.86$

Rejection region: $F > F_{\alpha/2, n_1, n_2} = F_{0.025, 49, 49} \approx F_{0.025, 50, 50} = 1.75$

or

$F < F_{1-\alpha/2, n_1, n_2} = F_{0.975, 49, 49} = 1/F_{0.025, 49, 49} \approx 1/F_{0.025, 50, 50} = 1/1.75 = .57$

Because $F = .86$ is not greater than 1.75 or smaller than .57, we cannot reject the null hypothesis.

EXCEL

	A	B	C
1	F-Test: Two-Sample for Variances		
2			
3		Direct	Broker
4	Mean	49.493	3.772
5	Variance	37.49	43.34
6	Observations	50	50
7	df	49	49
8	F	0.8650	
9	P(F<=f) one-tail	0.3068	
10	F Critical one-tail	0.6222	

The value of the test statistic is $F = .8650$. Excel outputs the one-tail p -value. Because we're conducting a two-tail test, we double that value. Thus, the p -value of the test we're conducting is $2 \times .3068 = .6136$.

INSTRUCTIONS

1. Type or import the data into two columns. (Open Xm13-01.)
2. Click **Data, Data Analysis**, and **F-test Two-Sample for Variances**.
3. Specify the **Variable 1 Range (A1:A51)** and the **Variable 2 Range (B1:B51)**. Type a value for α (.05).

MINITAB

Test for Equal Variances: Direct, Broker

F-Test (Normal Distribution)

Test statistic = 0.86, p-value = 0.614

INSTRUCTIONS

(Note: Some of the printout has been omitted.)

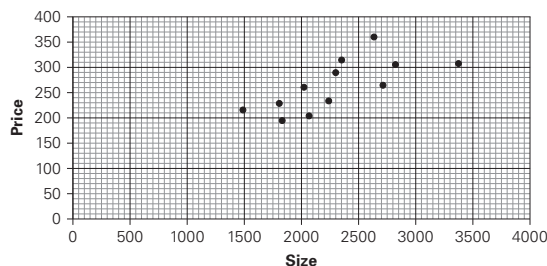
1. Type or import the data into two columns. (Open Xm13-01.)
2. Click **Stat, Basic Statistics**, and **2 Variances . . .**
3. In the **Samples in different columns** box, select the **First (Direct)** and **Second (Broker)** variables.

Manual calculation of the problem is presented first in each “Compute” section of the examples.

Step-by-step instructions in the use of Excel and Minitab immediately follow the manual presentation. Instruction appears in the book with the printouts—there’s no need to incur the extra expense of separate software manuals.

Appendix A provides summary statistics that allow students to solve applied exercises with data files by hand. Offering unparalleled flexibility, this feature allows virtually *all* exercises to be solved by hand!

APPENDIX A		
DATA FILE SAMPLE STATISTICS		
<p>Chapter 10</p> <p>10.30 $\bar{x} = 252.38$</p> <p>10.31 $\bar{x} = 1,610.16$</p> <p>10.32 $\bar{x} = 12.10$</p> <p>10.33 $\bar{x} = 10.21$</p> <p>10.34 $\bar{x} = -510$</p>	<p>12.108 $n(1) = 153, n(2) = 24$</p> <p>12.109 $n(1) = 92, n(2) = 28$</p> <p>12.110 $n(1) = 603, n(2) = 905$</p> <p>12.111 $n(1) = 92, n(2) = 334$</p> <p>12.112 $n(1) = 57, n(2) = 35, n(3) = 4, n(4) = 4$</p>	<p>13.27 Chitchat: $\bar{x}_1 = 654, s_1 = .048, n_1 = 95$</p> <p>Political: $\bar{x}_1 = 462, s_2 = .045, n_2 = 90$</p> <p>13.28 Planner: $\bar{x}_1 = 6.18, s_1 = 1.59, n_1 = 64$</p>



Ample use of graphics provides students many opportunities to see statistics in all its forms. In addition to manually presented figures throughout the text, Excel and Minitab graphic outputs are given for students to compare to their own results.

Interpret the Results



In the real world, it is not enough to know *how* to generate the statistics. To be truly effective, a business person must also know how to **interpret and articulate** the results. Furthermore, students need a framework to understand and apply statistics **within a realistic setting** by using realistic data in exercises, examples, and case studies.


Examples round out the final component of the identify–compute–interpret approach by asking students to interpret the results in the context of a business-related decision. This final step motivates and shows how statistics is used in everyday business situations.

An Applied Approach

With **Applications in ...** sections and boxes, *Statistics for Management and Economics* now includes 45 **applications** (in finance, marketing, operations management, human resources, economics, and accounting) highlighting how statistics is used in those professions. For example, “Applications in Finance: Portfolio Diversification and Asset Allocation” shows how probability is used to help select stocks to minimize risk. A new optional section, “Applications in Professional Sports: Baseball” contains a subsection on the success of the Oakland Athletics.

In addition to sections and boxes, **Applications in ... exercises** can be found within the exercise sections to further reinforce the big picture.

APPLICATIONS in OPERATIONS MANAGEMENT



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Quality

A critical aspect of production is quality. The quality of a final product is a function of the quality of the product's components. If the components don't fit, the product will not function as planned and likely cease functioning before its customers expect it to. For example, if a car door is not made to its specifications, it will not fit. As a result, the door will leak both water and air.

Operations managers attempt to maintain and improve the quality of products by ensuring that all components are made so that there is as little variation as possible. As you have already seen, statisticians measure variation by computing the variance.

Incidentally, an entire chapter (Chapter 21) is devoted to the topic of quality.

Nielsen Ratings

DATA
Xm12-00* Statistical techniques play a vital role in helping advertisers determine how many viewers watch the shows that they sponsor. Although several companies sample television viewers to determine what shows they watch, the best known is the A. C. Nielsen firm. The Nielsen ratings are based on a random sample of approximately 5,000 of the 115 million households in the United States with at least one television (in 2013). A meter attached to the televisions in the selected households keeps track of when the televisions are turned on and what channels they are tuned to. The data are sent to the Nielsen's computer every night from which Nielsen computes the rating and sponsors can determine the number of viewers and the potential value of any commercials. Of particular interest to advertisers are 18- to 49-year-olds, who are considered the most likely to buy advertised products. In 2013 there were 126.54 million Americans who were between 18 and 49 years old.



On page 415, we provide a solution to this problem.

Chapter-opening examples and solutions present compelling discussions of how the techniques and concepts introduced in that chapter are applied to real-world problems. These examples are then revisited with a solution as each chapter unfolds, applying the methodologies introduced in the chapter.

Nielsen Ratings: Solution

IDENTIFY

The problem objective is to describe the population of television shows watched by viewers across the country. The data are nominal. The combination of problem objective and data type make the parameter to be estimated the proportion of the entire population of 18- to 49-year-olds that watched *Big Bang Theory* (code = 2). The confidence interval estimator of the proportion is:

$$\hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}}$$

COMPUTE

MANUALLY:

To solve manually, we count the number of 2's in the file. We find this value to be 275. Thus,

$$\hat{p} = \frac{x}{n} = \frac{275}{5,000} = .0550$$

The confidence level is $1 - \alpha = .95$. It follows that $\alpha = .05$, $\alpha/2 = .025$, and $z_{\alpha/2} = z_{.025} = 1.96$.

The 95% confidence interval estimate of p is:

$$\hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}} = .0550 \pm 1.96 \sqrt{\frac{(.0550)(1 - .0550)}{5,000}} = .0550 \pm .0063$$

$$LCL = .0487 \quad UCL = .0613$$

EXCEL

	A	B
1	z-Estimate: Proportion	
2		TV Program
3	Sample Proportion	0.0550
4	Observations	5000
5	LCL	0.0487
6	UCL	0.0613

INSTRUCTIONS

1. Type or import the data into one column*. (Open Xm12-00.)
2. Click **Add-Ins, Data Analysis Plus**, and **Z-Estimate: Proportion**.
3. Specify the **Input Range (B1:B5001)**, the **Code for Success (2)**, and the value of α (.05).

MINITAB

Minitab requires that the data set contain only two values, the larger of which would be considered a success. In this example there are five values. If there are more than two codes or if the code for success is smaller than that for failure, we must recode.

Test and CI for One Proportion: Show				
Event = 4				
Variable	X	N	Sample p	95% CI
Programs	1319	5000	0.263800	(0.251585, 0.276015)
Using the normal approximation.				

*If the column contains a blank (representing missing data) the row will be deleted.

CASE 12.5 Bias in Roulette Betting

The game of roulette consists of a wheel with 38 colored and numbered slots. The numbers are 1 to 36, 0 and 00. Half of the slots numbered 1 to 36 are red and the other half are black. The two “zeros” are green. The wheel is spun and an iron ball is rolled, which eventually comes to rest in one of the slots. Gamblers can make several different kinds of bets. Most players bet on one or more numbers or on a color (black or red). Here is the layout of the roulette betting table:

0 3 6 9 12 15 18 21 24 27 30 33 36
 00 2 5 8 11 14 17 20 23 26 29 32 35
 1 4 7 10 13 16 19 22 25 28 31 34

Two statisticians recorded the bets on 904 spins. There were 21,731 bets. Researchers wanted to use these data to examine *middle bias*, which is the tendency for guessers in multiple-choice exams to select the middle answers. For example, if there are five choices a, b, c, d, and e, guessers will tend to select answer c. Most players stand on both sides of the betting table so that the middle numbers are 2, 5, 8, 11, 14, 17, 20, 23, 26, 29, 32, and 35.

a. If there is no middle bias, what proportion of the bets

- will be on 1 of the 12 middle numbers?
- b. Conduct a test at the 5% significance level to determine whether middle bias exists.
- c. The middle of the middle are the numbers 17 and 20. If there is no middle bias, what proportion of the bets will be either 17 or 20?
- d. Test with a 5% significance level to determine whether middle of the middle bias exists.

Source: Maya Bar-Hillel and Ro'i Zultan, “We Sing the Praise of Good Displays: How Gamblers Bet in Casino Roulette,” *Chance*, Volume 25, No. 2, 2012.

DATA
 C12-05

Many of the **examples, exercises, and cases** are based on **actual studies** performed by statisticians and published in journals, newspapers, and magazines, or presented at conferences. Many data files were recreated to produce the original results.

A total of 2,148 exercises, many of them new or updated, offer ample practice for students to use statistics in an applied context.

CHAPTER SUMMARY

This chapter introduced three statistical techniques. The first is the chi-squared goodness-of-fit test, which is applied when the problem objective is to describe a single population of nominal data with two or more categories. The second is the chi-squared test of a contingency table. This test has two objectives: to analyze the relationship between two nominal variables and to compare two or more populations of nominal data. The last procedure is designed to test for normality.

IMPORTANT TERMS:

Multinomial experiment	592	Cross-classification table	599
Chi-squared goodness-of-fit test	593	Chi-squared test of a contingency table	599
Expected frequency	593	Contingency table	602
Observed frequencies	594		

SYMBOLS:

Symbol	Pronounced	Represents
f_i	f sub i	Frequency of the i th category
e_i	e sub i	Expected value of the i th category
χ^2	Chi squared	Test statistic

FORMULA:

Test statistic for all procedures

$$\chi^2 = \sum_{i=1}^k \frac{(f_i - e_i)^2}{e_i}$$

COMPUTER OUTPUT AND INSTRUCTIONS:

Technique	Excel	Minitab
Chi-squared goodness-of-fit test	595	596
Chi-squared test of a contingency table (raw data)	604	604
Chi-squared test of a contingency table	604	604
Chi-squared test of normality	615	616

Instructor Resources

To access the instructor and student textbook resources, go to www.cengage.com/login, log in with your faculty account username and password, and use ISBN 9781285425450 to search for and to add instructor resources to your account.

Student Learning Resources

To access student textbook resources, go to www.cengagebrain.com and use ISBN 9781285425450 to access the **Data Analysis Plus** add-in, 992 data sets, optional topics, and 35 appendixes.

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WHAT IS STATISTICS?

- 1-1 *Key Statistical Concepts*
- 1-2 *Statistical Applications in Business*
- 1-3 *Large Real Data Sets*
- 1-4 *Statistics and the Computer*
- Appendix 1 *Instructions for Keller's website*

INTRODUCTION

Statistics is a way to get information from data. That's it! Most of this textbook is devoted to describing how, when, and why managers and statistics practitioners* conduct statistical procedures. You may ask, "If that's all there is to statistics, why is this book (and most other statistics books) so large?" The answer is that students of applied statistics will be exposed to different kinds of information and data. We demonstrate some of these with a case and two examples that are featured later in this book.

The first may be of particular interest to you.

*The term *statistician* is used to describe so many different kinds of occupations that it has ceased to have any meaning. It is used, for example, to describe a person who calculates baseball statistics as well as an individual educated in statistical principles. We will describe the former as a *statistics practitioner* and the

(continued)

EXAMPLE 3.3

Business Statistics Marks (See Chapter 3)

A student enrolled in a business program is attending his first class of the required statistics course. The student is somewhat apprehensive because he believes the myth that the course is difficult. To alleviate his anxiety, the student asks the professor about last year's marks. Because this professor is friendly and helpful, like all other statistics professors, he obliges the student and provides a list of the final marks, which are composed of term work plus the final exam. What information can the student obtain from the list?

This is a typical statistics problem. The student has the data (marks) and needs to apply statistical techniques to get the information he requires. This is a function of **descriptive statistics**.

Descriptive Statistics

Descriptive statistics deals with methods of organizing, summarizing, and presenting data in a convenient and informative way. One form of descriptive statistics uses graphical techniques that allow statistics practitioners to present data in ways that make it easy for the reader to extract useful information. In Chapters 2 and 3 we will present a variety of graphical methods.

Another form of descriptive statistics uses numerical techniques to summarize data. One such method that you have already used frequently calculates the average or mean. In the same way that you calculate the average age of the employees of a company, we can compute the mean mark of last year's statistics course. Chapter 4 introduces several numerical statistical measures that describe different features of the data.

The actual technique we use depends on what specific information we would like to extract. In this example, we can see at least three important pieces of information. The first is the "typical" mark. We call this a *measure of central location*. The average is one such measure. In Chapter 4, we will introduce another useful measure of central location, the median. Suppose the student was told that the average mark last year was 67. Is this enough information to reduce his anxiety? The student would likely respond "No" because he would like to know whether most of the marks were close to 67 or were scattered far below and above the average. He needs a *measure of variability*. The simplest such measure is the *range*, which is calculated by subtracting the smallest number from the largest. Suppose the largest mark is 96 and the smallest is 24. Unfortunately, this provides little information since it is based on only two marks. We need other measures—these will be introduced in Chapter 4. Moreover, the student must determine more about the marks. In particular, he needs to know how the marks are distributed between 24 and 96. The best way to do this is to use a graphical technique, the histogram, which will be introduced in Chapter 3.

latter as a *statistician*. A statistics practitioner is a person who uses statistical techniques properly. Examples of statistics practitioners include the following:

1. a financial analyst who develops stock portfolios based on historical rates of return;
2. an economist who uses statistical models to help explain and predict variables such as inflation rate, unemployment rate, and changes in the gross domestic product; and
3. a market researcher who surveys consumers and converts the responses into useful information.

Our goal in this book is to convert you into one such capable individual.

The term *statistician* refers to an individual who works with the mathematics of statistics. His or her work involves research that develops techniques and concepts that in the future may help the statistics practitioner. Statisticians are also statistics practitioners, frequently conducting empirical research and consulting. If you're taking a statistics course, your instructor is probably a statistician.

Case 12.1 Pepsi's Exclusivity Agreement with a University (see Chapter 12) In the last few years, colleges and universities have signed exclusivity agreements with a variety of private companies. These agreements bind the university to sell these companies' products exclusively on the campus. Many of the agreements involve food and beverage firms.

A large university with a total enrollment of about 50,000 students has offered Pepsi-Cola an exclusivity agreement that would give Pepsi exclusive rights to sell its products at all university facilities for the next year with an option for future years. In return, the university would receive 35% of the on-campus revenues and an additional lump sum of \$200,000 per year. Pepsi has been given 2 weeks to respond.

The management at Pepsi quickly reviews what it knows. The market for soft drinks is measured in terms of 12-ounce cans. Pepsi currently sells an average of 22,000 cans per week over the 40 weeks of the year that the university operates. The cans sell for an average of one dollar each. The costs, including labor, total 30 cents per can. Pepsi is unsure of its market share but suspects it is considerably less than 50%. A quick analysis reveals that if its current market share were 25%, then, with an exclusivity agreement, Pepsi would sell 88,000 (22,000 is 25% of 88,000) cans per week or 3,520,000 cans per year. The gross revenue would be computed as follows[†]:

$$\text{Gross revenue} = 3,520,000 \times \$1.00/\text{can} = \$3,520,000$$

This figure must be multiplied by 65% because the university would rake in 35% of the gross. Thus,

$$\begin{aligned} \text{Gross revenue after deducting 35\% university take} \\ = 65\% \times \$3,520,000 = \$2,288,000 \end{aligned}$$

The total cost of 30 cents per can (or \$1,056,000) and the annual payment to the university of \$200,000 are subtracted to obtain the net profit:

$$\text{Net profit} = \$2,288,000 - \$1,056,000 - \$200,000 = \$1,032,000$$

Pepsi's current annual profit is

$$40 \text{ weeks} \times 22,000 \text{ cans/week} \times \$0.70 = \$616,000$$

If the current market share is 25%, the potential gain from the agreement is

$$\$1,032,000 - \$616,000 = \$416,000$$

The only problem with this analysis is that Pepsi does not know how many soft drinks are sold weekly at the university. Coke is not likely to supply Pepsi with information about its sales, which together with Pepsi's line of products constitute virtually the entire market.

Pepsi assigned a recent university graduate to survey the university's students to supply the missing information. Accordingly, she organizes a survey that asks 500 students to keep track of the number of soft drinks they purchase in the next 7 days. The responses are stored in a file C12-01 available to be downloaded. See Appendix 1 for instructions.

Inferential Statistics

The information we would like to acquire in Case 12.1 is an estimate of annual profits from the exclusivity agreement. The data are the numbers of cans of soft drinks consumed in 7 days by the 500 students in the sample. We can use descriptive techniques to

[†]We have created an Excel spreadsheet that does the calculations for this case. See Appendix 1 for instructions on how to download this spreadsheet from Keller's website plus hundreds of data sets and much more.

learn more about the data. In this case, however, we are not so much interested in what the 500 students are reporting as in knowing the mean number of soft drinks consumed by all 50,000 students on campus. To accomplish this goal we need another branch of statistics: **inferential statistics**.

Inferential statistics is a body of methods used to draw conclusions or inferences about characteristics of populations based on sample data. The population in question in this case is the university's 50,000 students. The characteristic of interest is the soft drink consumption of this population. The cost of interviewing each student in the population would be prohibitive and extremely time consuming. Statistical techniques make such endeavors unnecessary. Instead, we can sample a much smaller number of students (the sample size is 500) and infer from the data the number of soft drinks consumed by all 50,000 students. We can then estimate annual profits for Pepsi.

EXAMPLE 12.5

Exit Polls (See Chapter 12)

When an election for political office takes place, the television networks cancel regular programming to provide election coverage. After the ballots are counted, the results are reported. However, for important offices such as president or senator in large states, the networks actively compete to see which one will be the first to predict a winner. This is done through **exit polls** in which a random sample of voters who exit the polling booth are asked for whom they voted. From the data, the sample proportion of voters supporting the candidates is computed. A statistical technique is applied to determine whether there is enough evidence to infer that the leading candidate will garner enough votes to win. Suppose that the exit poll results from the state of Florida during the year 2000 elections were recorded. Although several candidates were running for president, the exit pollsters recorded only the votes of the two candidates who had any chance of winning: Republican George W. Bush and Democrat Albert Gore. The results (765 people who voted for either Bush or Gore) were stored in file Xm12-05. The network analysts would like to know whether they can conclude that George W. Bush will win the state of Florida.

Example 12.5 describes a common application of statistical inference. The population the television networks wanted to make inferences about is the approximately 5 million Floridians who voted for Bush or Gore for president. The sample consisted of the 765 people randomly selected by the polling company who voted for either of the two main candidates. The characteristic of the population that we would like to know is the proportion of the Florida total electorate that voted for Bush. Specifically, we would like to know whether more than 50% of the electorate voted for Bush (counting only those who voted for either the Republican or Democratic candidate). It must be made clear that we cannot predict the outcome with 100% certainty because we will not ask all 5 million actual voters for whom they voted. This is a fact that statistics practitioners and even students of statistics must understand. A sample that is only a small fraction of the size of the population can lead to correct inferences only a certain percentage of the time. You will find that statistics practitioners can control that fraction and usually set it between 90% and 99%.

Incidentally, on the night of the United States election in November 2000, the networks goofed badly. Using exit polls as well as the results of previous elections, all four networks concluded at about 8 P.M. that Al Gore would win Florida. Shortly after 10 P.M., with a large percentage of the actual vote having been counted, the networks reversed course and declared that George W. Bush would win the state. By 2 A.M., another verdict was declared: The result was too close to call. Since then, this experience has likely been used by statistics instructors when teaching how *not* to use statistics.

Notice that, contrary to what you probably believed, data are not necessarily numbers. The marks in Example 3.3 and the number of soft drinks consumed in a week in Case 12.1, of course, are numbers; however, the votes in Example 12.5 are not. In Chapter 2, we will discuss the different types of data you will encounter in statistical applications and how to deal with them.

1-1 / KEY STATISTICAL CONCEPTS

Statistical inference problems involve three key concepts: the population, the sample, and the statistical inference. We now discuss each of these concepts in more detail.

1-1a Population

A **population** is the group of all items of interest to a statistics practitioner. It is frequently very large and may, in fact, be infinitely large. In the language of statistics, *population* does not necessarily refer to a group of people. It may, for example, refer to the population of ball bearings produced at a large plant. In Case 12.1, the population of interest consists of the 50,000 students on campus. In Example 12.5, the population consists of the Floridians who voted for Bush or Gore.

A descriptive measure of a population is called a **parameter**. The parameter of interest in Case 12.1 is the mean number of soft drinks consumed by all the students at the university. The parameter in Example 12.5 is the proportion of the 5 million Florida voters who voted for Bush. In most applications of inferential statistics the parameter represents the information we need.

1-1b Sample

A **sample** is a set of data drawn from the studied population. A descriptive measure of a sample is called a **statistic**. We use statistics to make inferences about parameters. In Case 12.1, the statistic we would compute is the mean number of soft drinks consumed in the last week by the 500 students in the sample. We would then use the sample mean to infer the value of the population mean, which is the parameter of interest in this problem. In Example 12.5, we compute the proportion of the sample of 765 Floridians who voted for Bush. The sample statistic is then used to make inferences about the population of all 5 million votes—that is, we predict the election results even before the actual count.

1-1c Statistical Inference

Statistical inference is the process of making an estimate, prediction, or decision about a population based on sample data. Because populations are almost always very large, investigating each member of the population would be impractical and expensive. It is far easier and cheaper to take a sample from the population of interest and draw conclusions or make estimates about the population on the basis of information provided by the sample. However, such conclusions and estimates are not always going to be correct. For this reason, we build into the statistical inference a measure of reliability. There are two such measures: the **confidence level** and the **significance level**. The *confidence level* is the proportion of times that an estimating procedure will be correct. For example, in Case 12.1, we will produce an estimate of the average number of soft drinks to be consumed by all 50,000 students that has a confidence level of 95%. In other words,

estimates based on this form of statistical inference will be correct 95% of the time. When the purpose of the statistical inference is to draw a conclusion about a population, the *significance level* measures how frequently the conclusion will be wrong. For example, suppose that, as a result of the analysis in Example 12.5, we conclude that more than 50% of the electorate will vote for George W. Bush, and thus he will win the state of Florida. A 5% significance level means that samples that lead us to conclude that Bush wins the election will be wrong 5% of the time.

1-2 / STATISTICAL APPLICATIONS IN BUSINESS

An important function of statistics courses in business and economics programs is to demonstrate that statistical analysis plays an important role in virtually all aspects of business and economics. We intend to do so through examples, exercises, and cases. However, we assume that most students taking their first statistics course have not taken courses in most of the other subjects in management programs. To understand fully how statistics is used in these and other subjects, it is necessary to know something about them. To provide sufficient background to understand the statistical application we introduce applications in accounting, economics, finance, human resources management, marketing, and operations management. We will provide readers with some background to these applications by describing their functions in two ways.

1-2a Application Sections and Subsections

We feature five sections that describe statistical applications in the functional areas of business. For example, in Section 7-3 we show an application in finance that describes a financial analyst's use of probability and statistics to construct portfolios that decrease risk.

One section and one subsection demonstrate the uses of probability and statistics in specific industries. Section 4-5 introduces an interesting application of statistics in professional baseball. A subsection in Section 6-4 presents an application in medical testing (useful in the medical insurance industry).

1-2b Application Boxes

For other topics that require less detailed description, we provide application boxes with a relatively brief description of the background followed by examples or exercises. These boxes are scattered throughout the book. For example, in Chapter 3 we discuss a job a marketing manager may need to undertake to determine the appropriate price for a product. To understand the context, we need to provide a description of marketing management. The statistical application will follow.

1-3 / LARGE REAL DATA SETS

The authors believe that you learn statistics by doing statistics. For their lives after college and university, we expect our students to have access to large amounts of real data that must be summarized to acquire the information needed to make decisions. To provide practice in this vital skill we have created eight large real data sets, available to be downloaded from Keller's website. Their sources are the General Social Survey (GSS) and the American National Election Survey (ANES).

1-3a General Social Survey

Since 1972, the GSS has been tracking American attitudes on a wide variety of topics. With the exception of the U.S. Census, the GSS is the most frequently used source of information about American society. The surveys now conducted every second year measure hundreds of variables and thousands of observations. We have included the results of the last six surveys (years 2002, 2004, 2006, 2008, 2010, and 2012), stored as GSS2002, GSS2004, GSS2006, GSS2008, GSS2010, and GSS2012, respectively. The survey sizes are 2,765, 2,812, 4,510, 2,023, 2,044, and 1,974, respectively. We have reduced the number of variables to about 60 and have deleted the responses that are known as missing data (don't know, refused, etc.).

We have included some demographic variables, such as age, gender, race, income, and education. Other variables measure political views, support for various government activities, and work. The full lists of variables for each year are stored on our website in Appendixes GSS2002, GSS2004, GSS2006, GSS2008, GSS2010, and GSS2012.

We have scattered examples and exercises from these data sets throughout this book.

1-3b American National Election Survey

The goal of the American National Election Survey is to provide data about why Americans vote as they do. The surveys are conducted in presidential election years. We have included data from the 2004 and 2008 surveys. Like the GSS, the ANES includes demographic variables. It also deals with interest in the presidential election as well as variables describing political beliefs and affiliations. Online Appendixes ANES2004 and ANES2008 contain the names and definitions of the variables.

The 2008 surveys overly sampled African American and Hispanic voters. We have “adjusted” these data by randomly deleting responses from these two racial groups.

As is the case with the GSSs, we have removed missing data.

1-4 / STATISTICS AND THE COMPUTER

In virtually all applications of statistics, the statistics practitioner must deal with large amounts of data. For example, Case 12.1 (Pepsi-Cola) involves 500 observations. To estimate annual profits, the statistics practitioner would have to perform computations on the data. Although the calculations do not require any great mathematical skill, the sheer amount of arithmetic makes this aspect of the statistical method time-consuming and tedious.

Fortunately, numerous commercially prepared computer programs are available to perform the arithmetic. We have chosen to use Microsoft Excel, which is a spreadsheet program, and Minitab, which is a statistical software package. (We use the latest versions of both software: Office 2013 and Minitab 16.) We chose Excel because we believe that it is and will continue to be the most popular spreadsheet package. One of its drawbacks is that it does not offer a complete set of the statistical techniques we introduce in this book. Consequently, we created add-ins that can be loaded onto your computer to enable you to use Excel for all statistical procedures introduced in this book. The add-ins can be downloaded and, when installed, will appear as *Data Analysis Plus*® on Excel's Add-Ins menu. Also available are introductions to Excel and Minitab, and detailed instructions for both software packages.

Appendix 1 describes the material that can be downloaded and provides instructions on how to acquire the various components.

A large proportion of the examples, exercises, and cases feature large data sets. These are denoted with the file name next to the exercise number. We demonstrate the solution to the statistical examples in three ways: manually, by employing Excel, and by using Minitab. Moreover, we will provide detailed instructions for all techniques.

The files contain the data needed to produce the solution. However, in many real applications of statistics, additional data are collected. For instance, in Example 12.5, the pollster often records the voter's gender and asks for other information including race, religion, education, and income. Many other data sets are similarly constructed. In later chapters, we will return to these files and require other statistical techniques to extract the needed information. (Files that contain additional data are denoted by an asterisk on the file name.)

The approach we prefer to take is to minimize the time spent on manual computations and to focus instead on selecting the appropriate method for dealing with a problem and on interpreting the output after the computer has performed the necessary computations. In this way, we hope to demonstrate that statistics can be as interesting and as practical as any other subject in your curriculum.

1-4a Excel Spreadsheets

Books written for statistics courses taken by mathematics or statistics majors are considerably different from this one. It is not surprising that such courses feature mathematical proofs of theorems and derivations of most procedures. When the material is covered in this way, the underlying concepts that support statistical inference are exposed and relatively easy to see. However, this book was created for an applied course in business and economics statistics. Consequently, we do not address directly the mathematical principles of statistics. However, as we pointed out previously, one of the most important functions of statistics practitioners is to properly interpret statistical results, whether produced manually or by computer. And, to correctly interpret statistics, students require an understanding of the principles of statistics.

To help students understand the basic foundation, we will teach readers how to create Excel spreadsheets that allow for *what-if* analyses. By changing some of the input value, students can see for themselves how statistics works. (The term is derived from *what* happens to the statistics *if* I change this value?) These spreadsheets can also be used to calculate many of the same statistics that we introduce later in this book.

CHAPTER SUMMARY

IMPORTANT TERMS:

Descriptive statistics 2
 Inferential statistics 4
 Exit polls 4
 Population 5
 Parameter 5

Sample 5
 Statistic 5
 Statistical inference 5
 Confidence level 5
 Significance level 5

CHAPTER EXERCISES

- 1.1** In your own words, define and give an example of each of the following statistical terms.
- population
 - sample
 - parameter
 - statistic
 - statistical inference
- 1.2** Briefly describe the difference between descriptive statistics and inferential statistics.
- 1.3** A politician who is running for the office of mayor of a city with 25,000 registered voters commissions a survey. In the survey, 48% of the 200 registered voters interviewed say they plan to vote for her.
- What is the population of interest?
 - What is the sample?
 - Is the value 48% a parameter or a statistic? Explain.
- 1.4** A manufacturer of computer chips claims that less than 10% of its products are defective. When 1,000 chips were drawn from a large production, 7.5% were found to be defective.
- What is the population of interest?
 - What is the sample?
 - What is the parameter?
 - What is the statistic?
 - Does the value 10% refer to the parameter or to the statistic?
 - Is the value 7.5% a parameter or a statistic?
 - Explain briefly how the statistic can be used to make inferences about the parameter to test the claim.
- 1.5** Suppose you believe that, in general, graduates who have majored in *your* subject are offered higher salaries upon graduating than are graduates of other programs. Describe a statistical experiment that could help test your belief.
- 1.6** You are shown a coin that its owner says is fair in the sense that it will produce the same number of heads and tails when flipped a very large number of times.
- Describe an experiment to test this claim.
 - What is the population in your experiment?
 - What is the sample?
 - What is the parameter?
 - What is the statistic?
 - Describe briefly how statistical inference can be used to test the claim.
- 1.7** Suppose that in Exercise 1.6 you decide to flip the coin 100 times.
- What conclusion would you be likely to draw if you observed 95 heads?
 - What conclusion would you be likely to draw if you observed 55 heads?
 - Do you believe that, if you flip a perfectly fair coin 100 times, you will always observe exactly 50 heads? If you answered “no,” then what numbers do you think are possible? If you answered “yes,” how many heads would you observe if you flipped the coin twice? Try flipping a coin twice and repeating this experiment 10 times and report the results.
- 1.8** **Xr01-08** The owner of a large fleet of taxis is trying to estimate his costs for next year's operations. One major cost is fuel purchases. To estimate fuel purchases, the owner needs to know the total distance his taxis will travel next year, the cost of a gallon of fuel, and the fuel mileage of his taxis. The owner has been provided with the first two figures (distance estimate and cost of a gallon of fuel). However, because of the high cost of gasoline, the owner has recently converted his taxis to operate on propane. He has measured and recorded the propane mileage (in miles per gallon) for 50 taxis.
- What is the population of interest?
 - What is the parameter the owner needs?
 - What is the sample?
 - What is the statistic?
 - Describe briefly how the statistic will produce the kind of information the owner wants.